

PRESENTING JIMI:

A HOPPING MONOPOD ROBOT INCORPORATING NONLINEAR
SERIES ELASTIC ACTUATORS, FIBER-REINFORCED POLYMER
CONSTRUCTION, AND A CONCURRENT ASYNCHRONOUS
DATAFLOW-BASED CENTROIDAL MOMENTUM BALANCE
CONTROLLER

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THE TOPIC OF THIS PRESENTATION

NAME: JIMI

MASS: 8.3kg (minimally)
10.9kg (autonomous)

SIZE: ~95cm tall, 27cm shank,
40cm thigh, 51cm body

SPEED: 1.0 m/s, 2.1 hops/sec
(design goals, not yet reached)

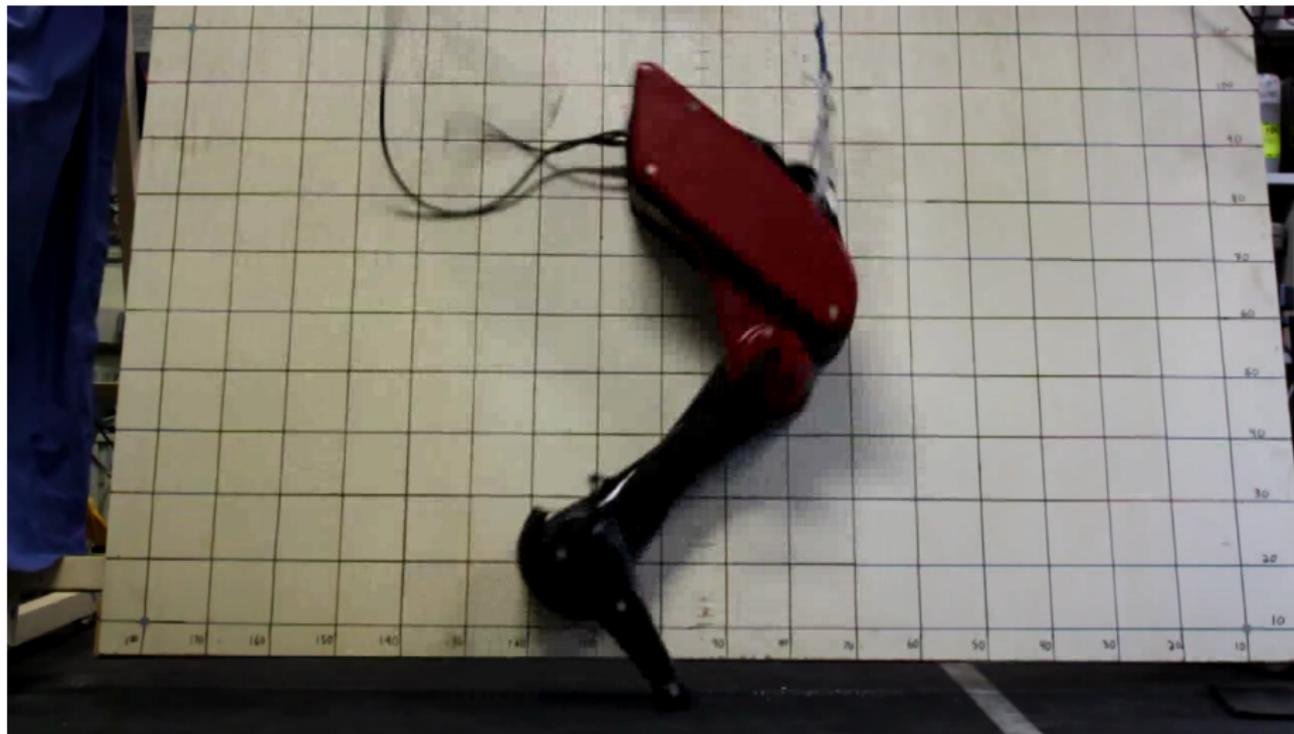
HEIGHT: Jumps 36cm vertically
(from squat, uncontrolled)

POWER: 2x111W electric motors

ENERGY: 2x27J elastic energy storage



PRELIMINARY TEASER VIDEO



PRESENTATION ROADMAP

“JIMI” integrates many details into a state-of-the-art robot:

DYNAMICS: Mechanical and control dynamics were designed simultaneously via simulation

ACTUATION: Uses novel, patented nonlinear series elastic actuators

CONTROL: Balances dynamically via task-space control of centroid

ESTIMATION: Performs online, model-based system identification

SOFTWARE: Software is asynchronous, dataflow-based & concurrent

MATERIALS: Features lightweight, monocoque structures made of CFRP (Carbon fiber-reinforced polymer) and urethane foam

This presentation will take about 25 minutes.

PART I: THE DYNAMICS OF RUNNING

Goal: To proceed analytically from animal-like sinusoidal vertical ground reaction forces (GRFs) to a specification of actuation and control for JIMI.

Overview:

1. Dynamics of animal running
2. A simplified model of running
3. How dynamics lead to actuation specification

DYNAMICS OF ANIMAL RUNNING

What *best* characterizes running?

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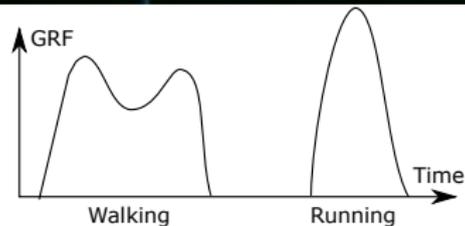
- ▶ No feet touching the ground?



DYNAMICS OF ANIMAL RUNNING

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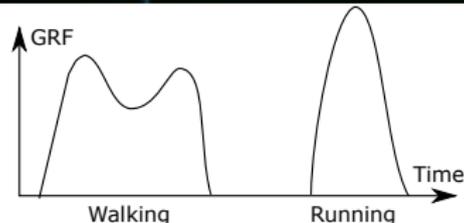
- ▶ No feet touching the ground?
- ▶ A single-hump vertical GRF?



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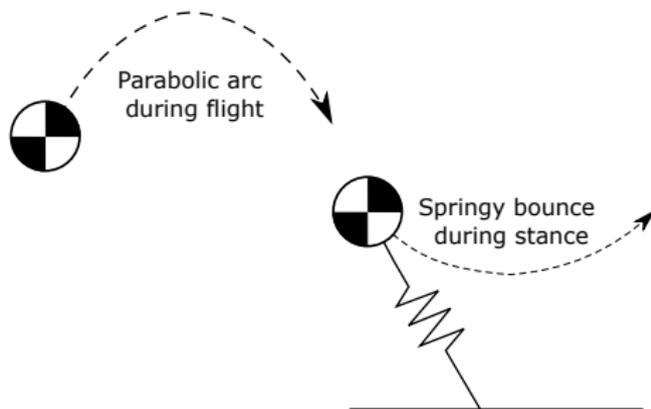
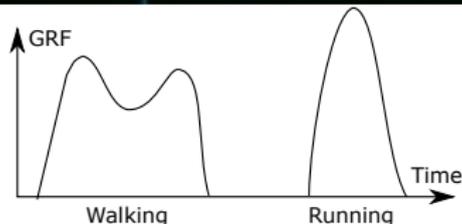
- ▶ No feet touching the ground?
- ▶ A single-hump vertical GRF?
- ▶ Flight Center of Mass (CoM) motion that's ballistic?



DYNAMICS OF ANIMAL RUNNING

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- ▶ Stance forces that resemble an elastic collision?



DYNAMICS OF ANIMAL RUNNING

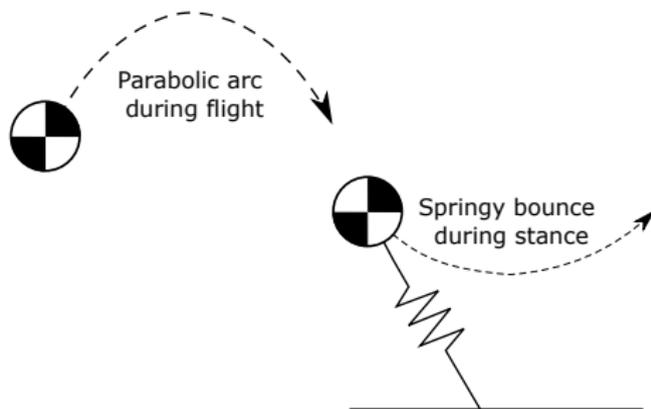
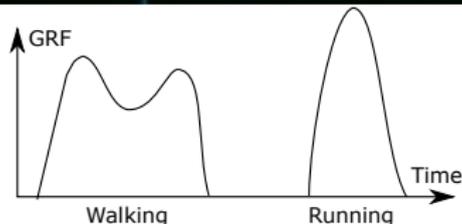
What *best* characterizes running?

- ▶ No feet touching the ground?
- ▶ A single-hump vertical GRF?
- ▶ Flight Center of Mass (CoM) motion that's ballistic?
- ▶ Stance forces that resemble an elastic collision?

Animals exhibit all the above.

The design of JIMI assumes a *GRF resembling an elastic collision* is key.

Can we get a rough spec from this?



PEAK GRF FOR ELASTIC GRFs

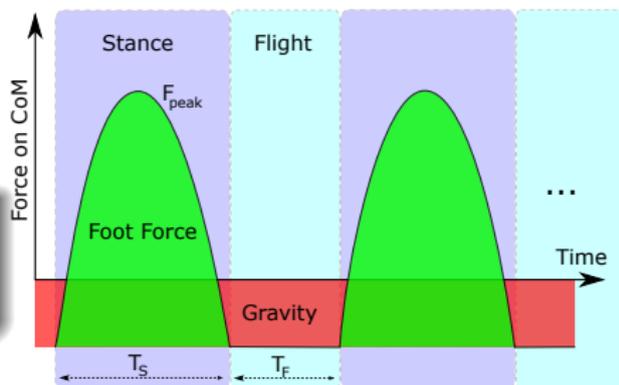
The sum of all impulses to the CoM should be zero over a stride.

IMPULSE DUE TO GRF

$$I_S = \int_0^{T_S} F_{peak} \sin\left(\frac{\pi}{T_S} t\right) dt$$

IMPULSE DUE TO GRAVITY

$$I_g = m_c g (T_S + T_F)$$



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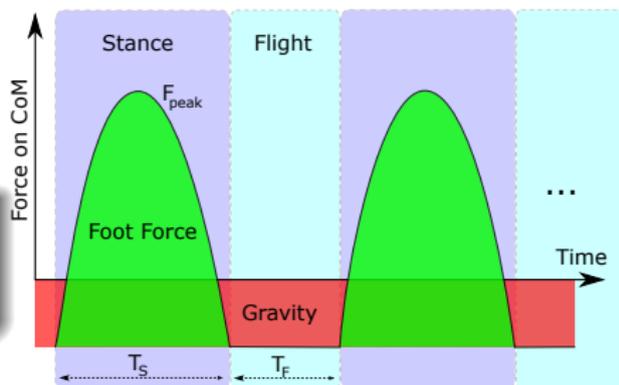
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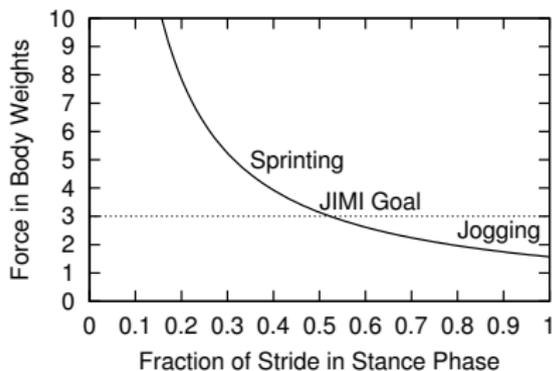
PEAK GRF

$$F_{peak}(T_S, T_F) = \frac{\pi m_c g (T_S + T_F)}{2T_S}$$

JIMI Goal: 50% stance, $\sim 3B.W.$



Peak Ground Force vs Stance Fraction



CoM POWER AND ENERGY IN STANCE

CoM HEIGHT

$$y_c(t) = \begin{cases} \frac{gt^2}{2} + \dot{y}_c^{LO} t & \text{(flight)} \\ \frac{(g + \frac{F_{peak}}{m_c} \sin(\frac{\pi}{T_S} t))t^2}{2} + \dot{y}_c^{TD} t & \text{(stance)} \end{cases}$$

GRF POWER ON CoM

$$P(t) = F_f(t)\dot{y}_c(t)$$

CoM ENERGY CHANGE

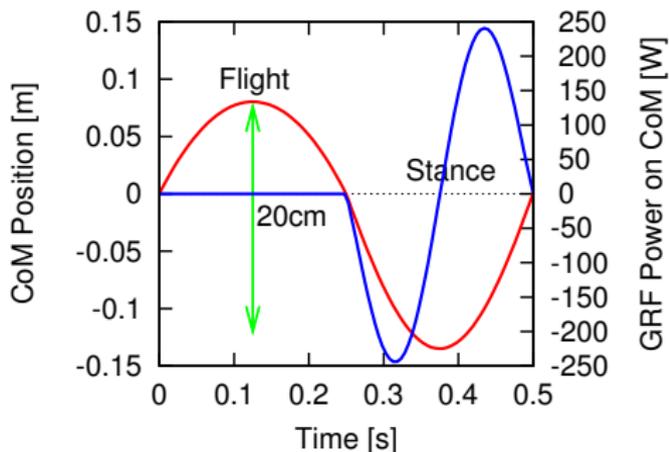
$$\Delta V(y_c) = m_c g \Delta y_c$$

For a 10kg robot with 0.25s stance and flight times:

- ▶ ~20cm total vertical motion
- ▶ ~20J absorb/release per hop
- ▶ ~250W peak mech. power

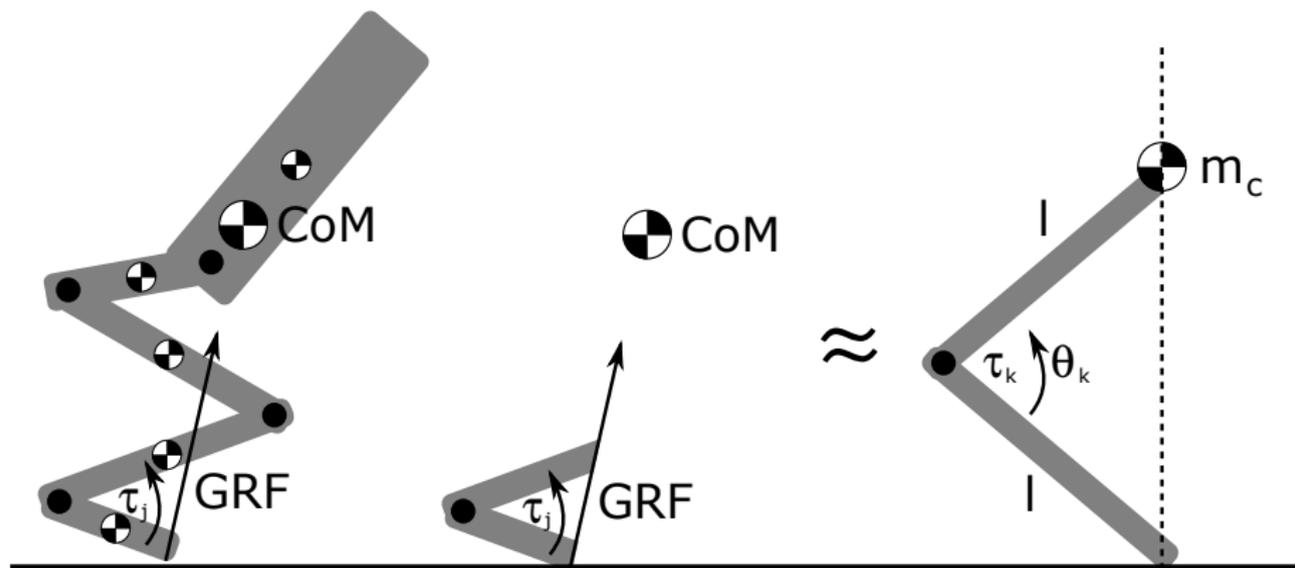
How would joint torques look?

CoM Position and GRF Power vs Time



REVOLUTE-JOINTED RUNNERS

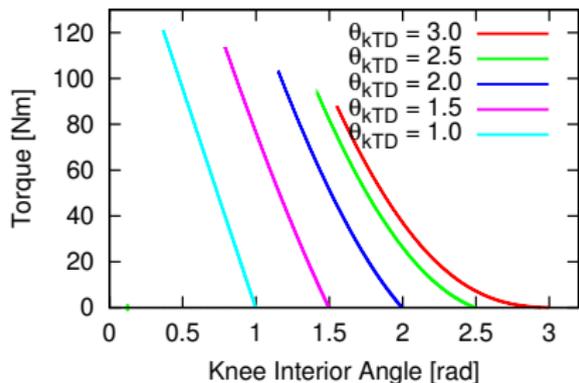
Joint torques can be estimated from GRF vector and simple kinematics.



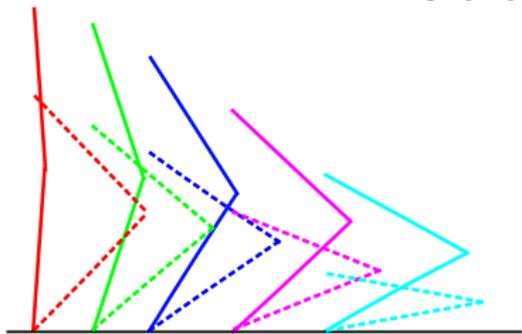
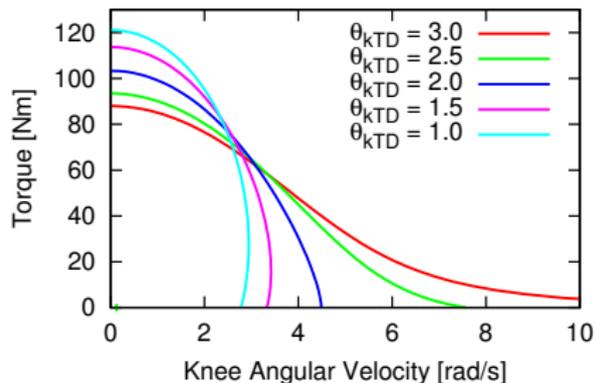
The model on the right is a reasonable general case approximation.
(We ignore moments of inertia and link length asymmetries)

ACTUATOR TORQUE/VELOCITY REQUIREMENTS

Knee Torque vs Angle for Sinusoidal GRF



Knee Torque vs Ang. Velocity for Sinusoidal GRF



- ▶ Let $m_c = 10\text{kg}$, $l = 0.4\text{m}$, 2Hz hop, 50% stance duty cycle
- ▶ Torques $< 120\text{Nm}$ torque
- ▶ Velocity $< 10\text{rad/s}$
- ▶ Straighter legs more nonlinear

SUMMARY OF RUNNING DYNAMICS

Assuming an elastic vertical GRF gave us:

- ▶ CoM motion
- ▶ CoM power & energy
- ▶ Peak GRF levels

Assuming revolute joints gave us:

- ▶ Rough character of joint torque nonlinearity
- ▶ Velocity, torque limits

Can we now design an actuator that satisfies the above specs?

PART II: NONLINEAR SERIES ELASTIC ACTUATION

Goal: To present two novel, nonlinear series elastic actuators ideal for legged robots.

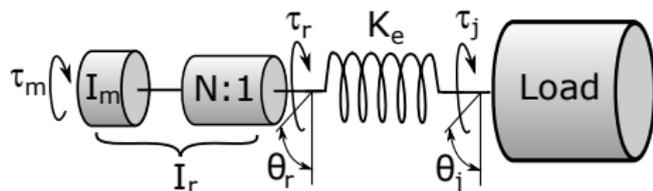
Overview:

1. Introduction to Series Elasticity
2. Optimal Series Elasticity
3. The Hypocycloid Mechanism
4. The HypoSEA-v1
5. The HypoSEA-v2



WHAT IS A SERIES ELASTIC ACTUATOR? (SEA)

SEAs purposely introduce an elastic element between actuator and load.



Good effects:

- ▶ Improves L.F. force control
- ▶ Improves impact resistance
- ▶ Provides energy storage

Bad effects:

- ▶ Reduces force bandwidth
- ▶ Adds another DOF
- ▶ Naive controllers often waste work compressing elasticity

TRANSMISSION EFFECTS

$$\tau_r = N\tau_m$$

$$I_r = N^2 I_m$$

NORMAL DYNAMIC STIFFNESS

$$\frac{\tau_j}{\theta_j} = N^2 I_m s^2$$

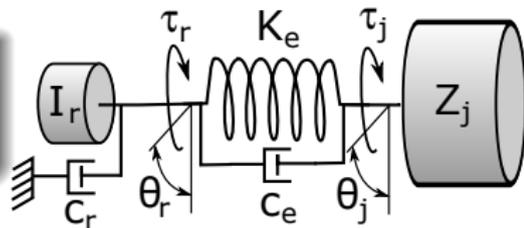
SEA DYNAMIC STIFFNESS

$$\frac{\tau_j}{\theta_j} = K_e$$

FREQUENCY DOMAIN ANALYSIS (*Williamson, 1995*)

COMPLEX ROTOR TORQUE

$$\tau_r(\tau_j, \dot{\theta}_j) = \left(\frac{I_r s^2 + c_r s}{c_e s + K_e} + 1 \right) \tau_j + (I_r s + c_r) \dot{\theta}_j$$



Conclusions:

- ▶ Only the **red terms** are unique to SEAs.

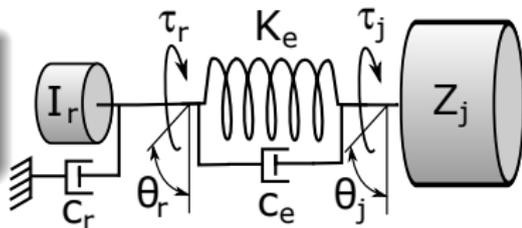
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Let $s = j\omega$, $c_r = c_e = 0$ to see spring effect:

$$\tau_r(\tau_j, \dot{\theta}_j) = \left(1 - \frac{I_r \omega^2}{K_e} \right) \tau_j + j I_r \omega \dot{\theta}_j$$



Conclusions:

- ▶ Only the **red terms** are unique to SEAs.
- ▶ Rotor-elastic resonance at $\sqrt{\frac{K_e}{I_r}}$

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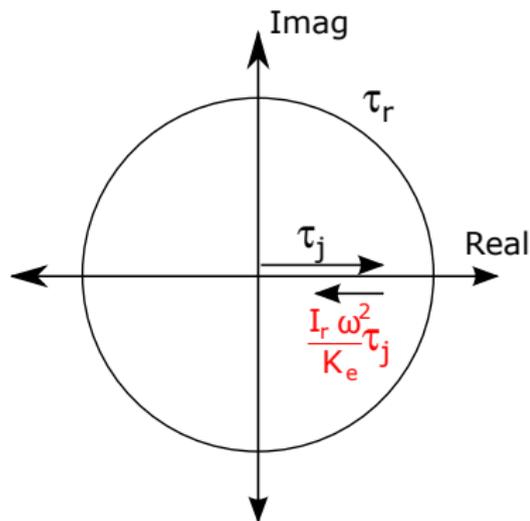
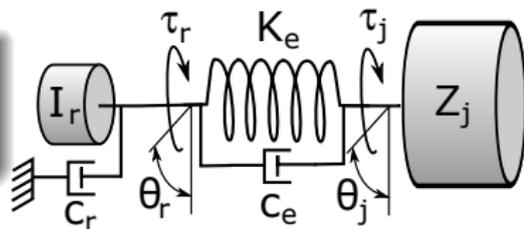
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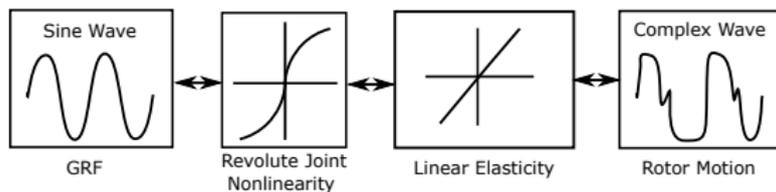
Conclusions:

- ▶ Only the **red terms** are unique to SEAs.
- ▶ Rotor-elastic resonance at $\sqrt{\frac{K_e}{I_r}}$
- ▶ Spring reduces τ_r for $\omega < \sqrt{2\frac{K_e}{I_r}}$
- ▶ More rotor torque “left over” to track load motion \implies better force control



WHAT ABOUT NONLINEARITIES?

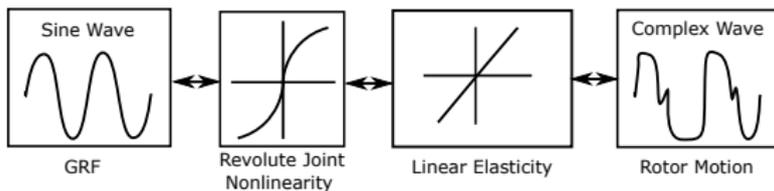
Problem: Running joint torques are nonlinear \implies excess rotor motion.



To maximize control torque available for counteracting disturbances, we want the rotor motion simple and harmonic.

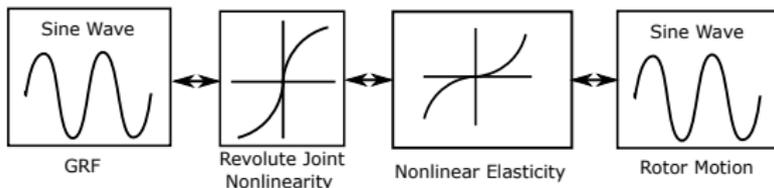
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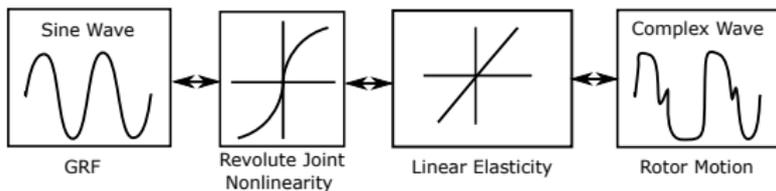
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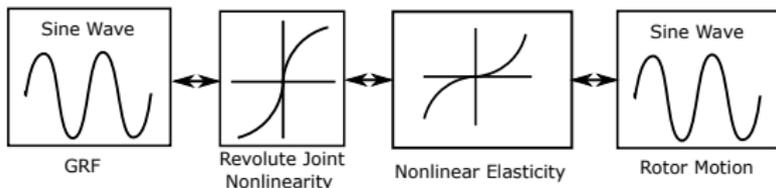
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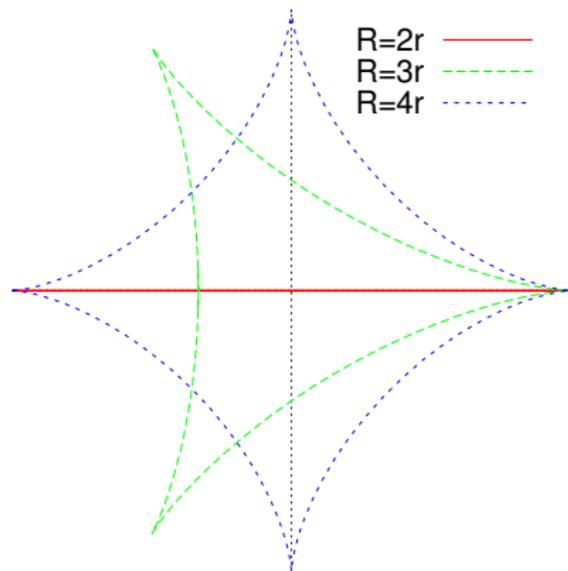
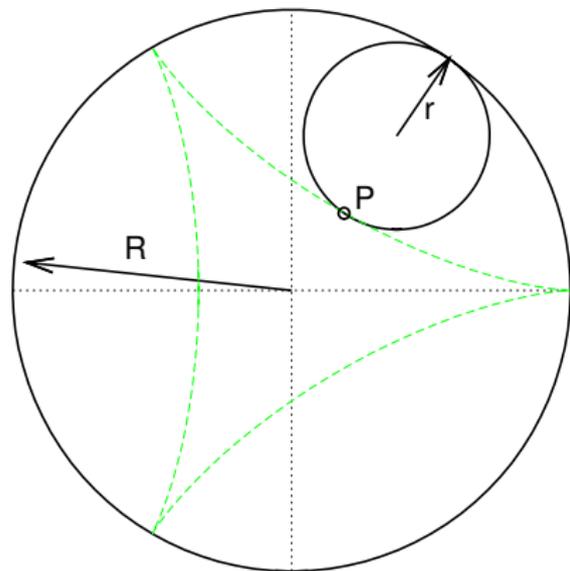
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What mechanisms produce the proper nonlinear elasticity for running?

WHAT'S A HYPOCYCLOID?

The curve traced by a point on a small circle rolling inside a larger circle.



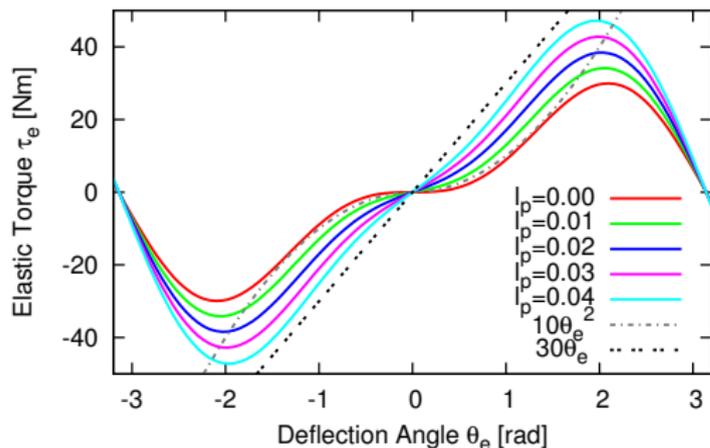
If $R = 2r$, a straight line is drawn from a revolute motion.

HYPOCYCLOID-BASED SERIES ELASTIC ACTUATOR

TORQUE-ANGLE RELATION

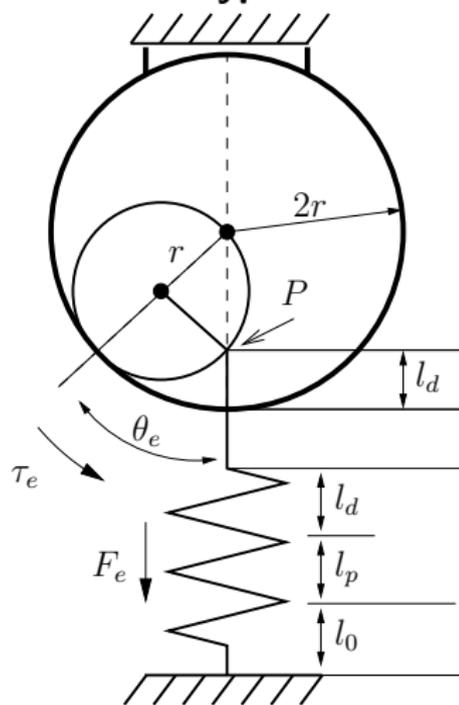
$$\tau_e(\theta_e) = 2rK_e(2r(1 - \cos \theta_e) + l_p) \sin \theta_e$$

Torque vs Deflection for Hypocycloid Mechanism



Varying the spring pretension l_p produces a useful family of curves for running robots!

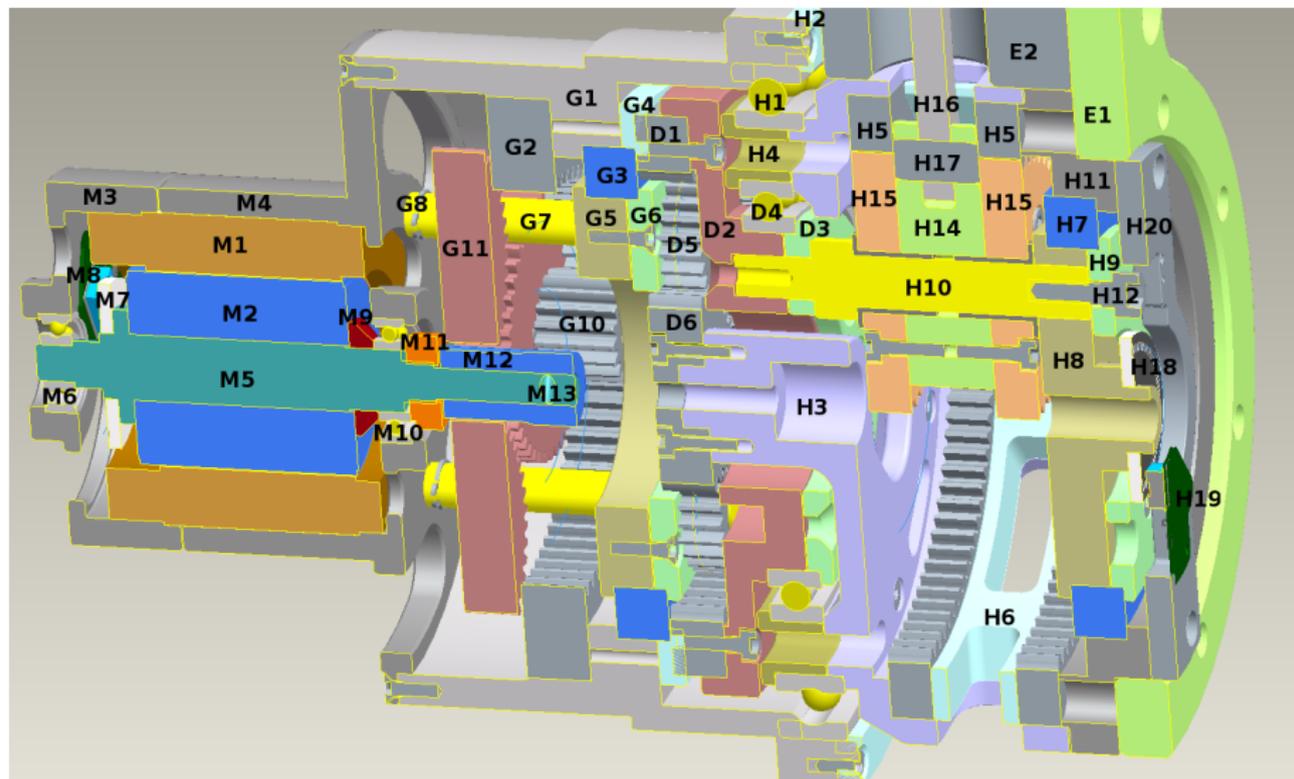
The HypoSEA:



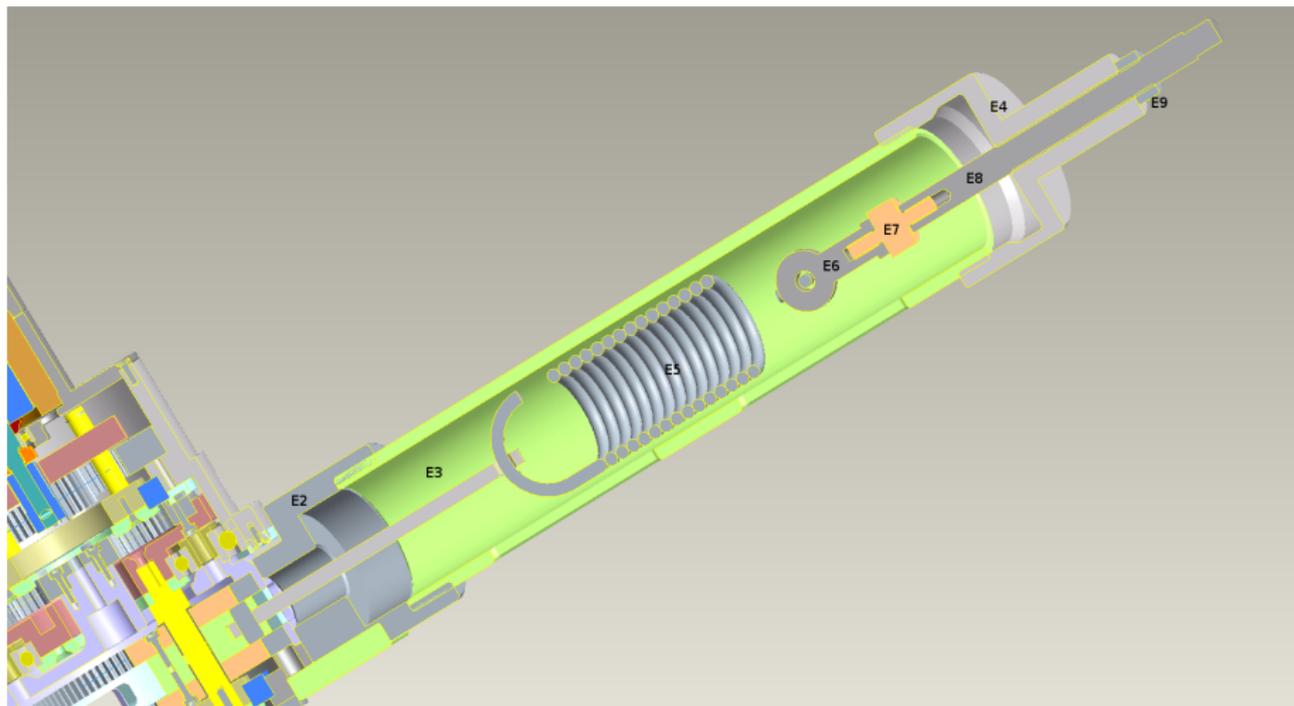
HYPOSEA-v1 PHOTO



HYPOSEA-v1 CROSS SECTION



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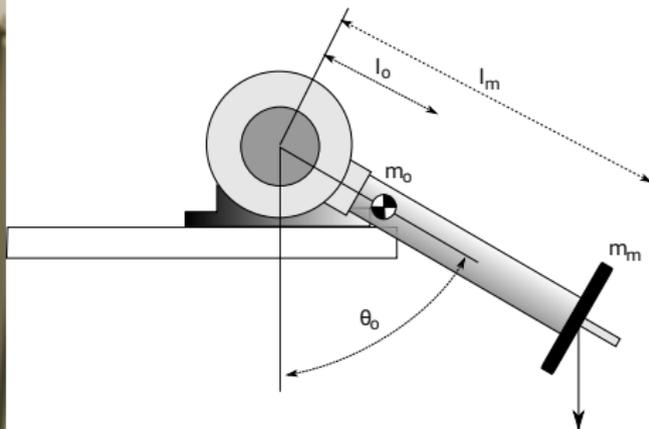


HYPOSEA-v1 VIDEO



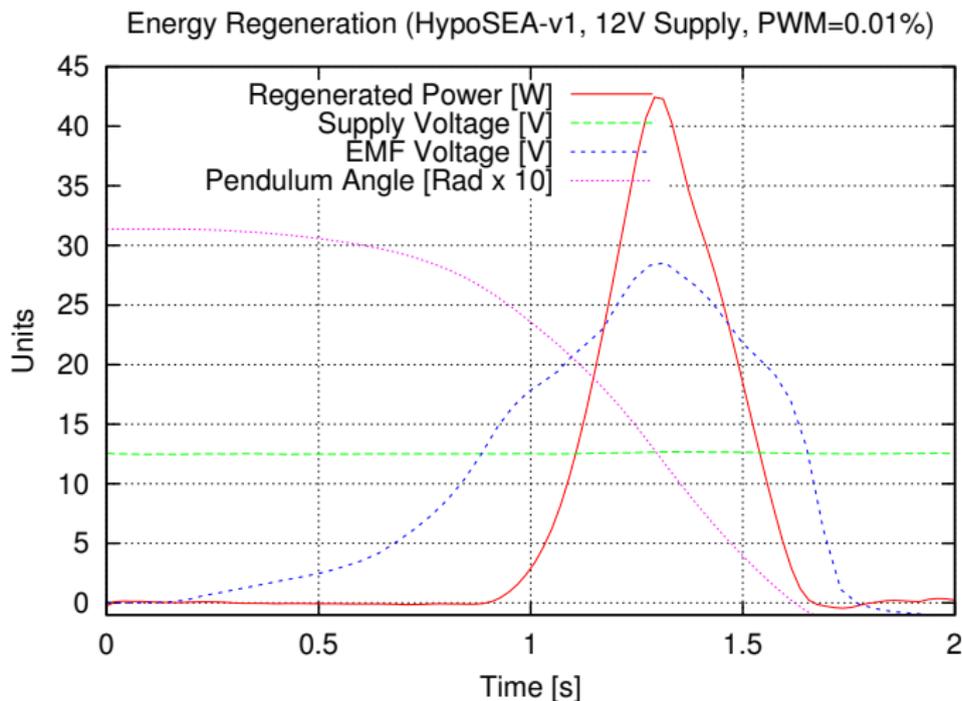
BACKDRIVABILITY \implies ENERGY RECOVERY

Experiment: How much energy can be recovered from a pendulum swing?



If a lead-acid battery is used as a power supply, when the BLDC motor spins fast enough, current flows into the battery even with a naive motor control board. Let's attach a 2kg mass and measure the energy absorbed.

HYPOSEA-v1 ENERGY RECOVERY (65% EFF.)



Absorbed 13.7J of a possible 21.0J (excluding K.E. lost below EMF=13V).

HYPOSEA-v1 PERFORMANCE RESULTS

The Good:

- ▶ Low passive mechanical impedance
- ▶ Impact resistance
- ▶ Backdrivability
- ▶ Energy regeneration efficiency (65%)
- ▶ Energy storage if rotor locked ($>40\text{J}$)

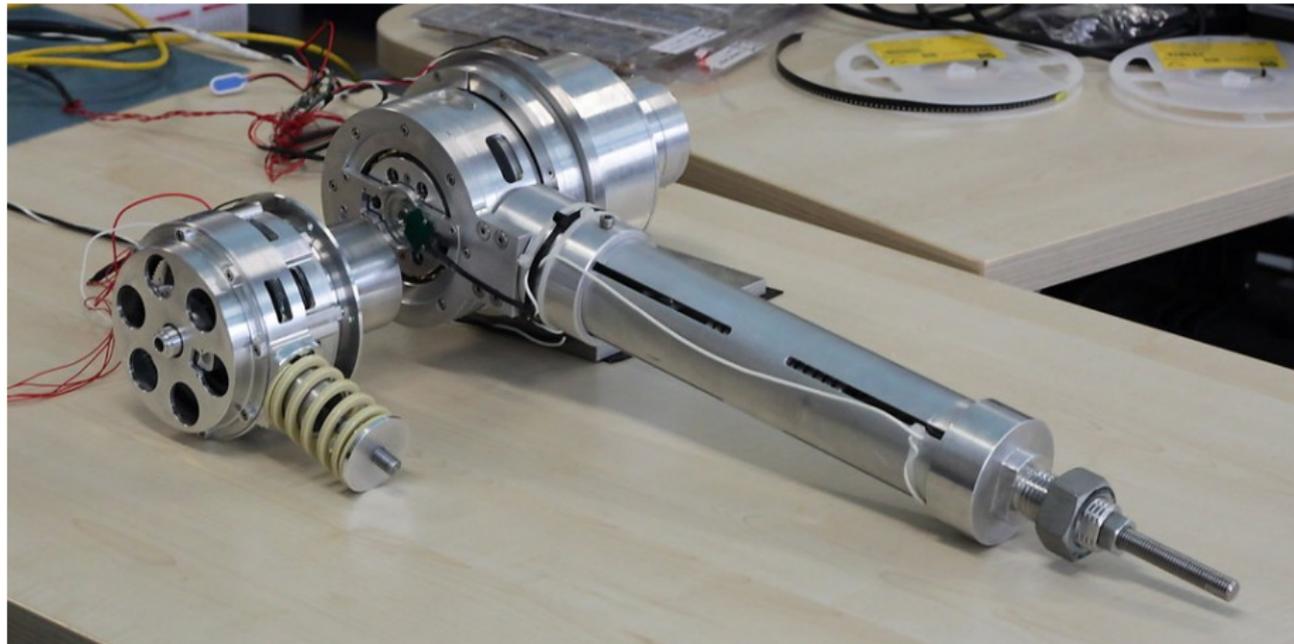
The Bad:

- ▶ Heavy (8.5kg)
- ▶ Big (0.5m)
- ▶ Too much friction (1-2Nm)
- ▶ Too little momentary torque (71Nm...goal was 120Nm)

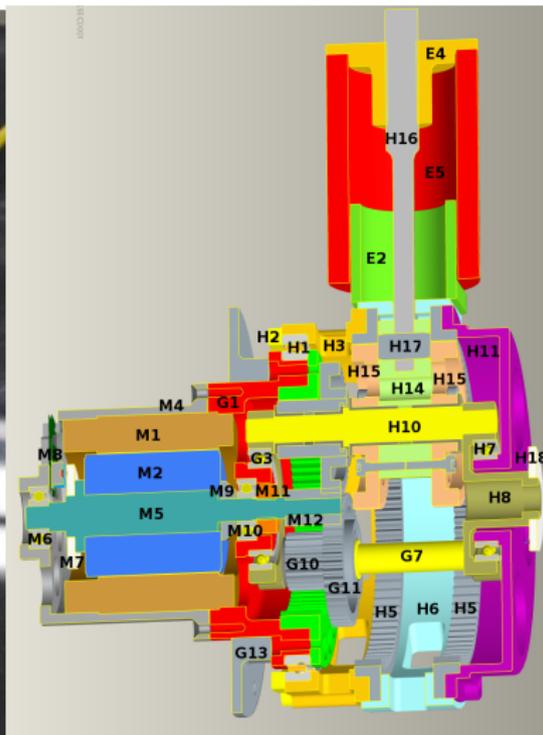
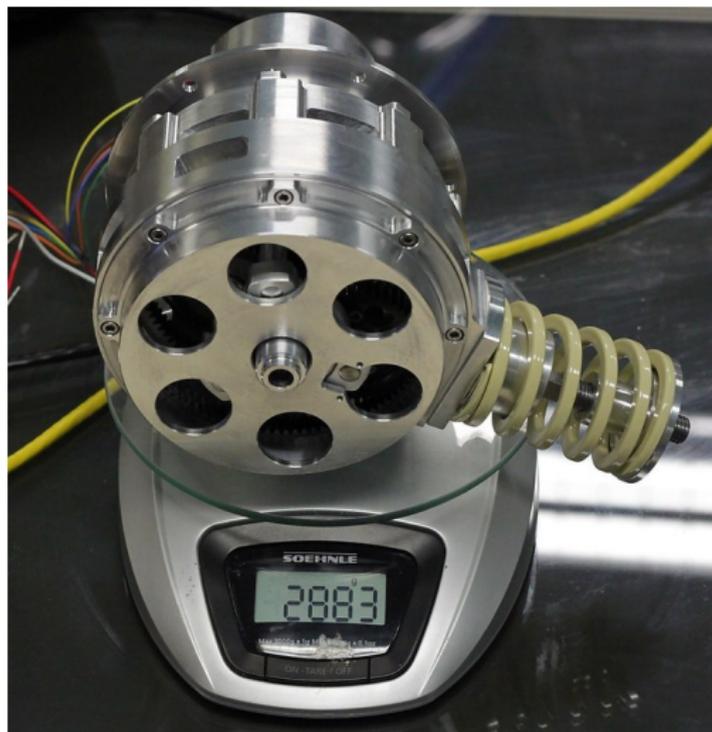
A second revision was clearly needed!

HYPOSEA-v2 PHOTO COMPARISON

The HypoSEA-v2 (left) is the improved version of the HypoSEA-v1 (right).



HYPOSEA-v2 INSIDE AND OUT



HYPOSEA PERFORMANCE COMPARISON

Description	v1	v2	Unit
Actuator mass	8.3	2.883	kg
Actuator diameter	14.0	12.4	cm
Longest exterior dimension	67	21	cm
Max tested joint torque	71	65	Nm
Max theoretical joint torque	126	70	Nm
Min resolvable torque	<0.02	<0.02	Nm
Max controlled joint vel	10.2	10.6	rad/s
Rotor-joint Gear Ratio	18. $\bar{3}$	17	
Elasticity-Rotor Gear Ratio	12.8 $\bar{3}$	17	
Joint-Elasticity Gear Ratio	$\frac{10}{7}$	1	
Linear Spring Constant	10.09	30.82	N/mm
Max spring pretension	40	20	mm
Max spring deflection	72	48	mm
Hypocycloid gear radius	24	24	mm
Max spring energy*	42.3	27.3	J

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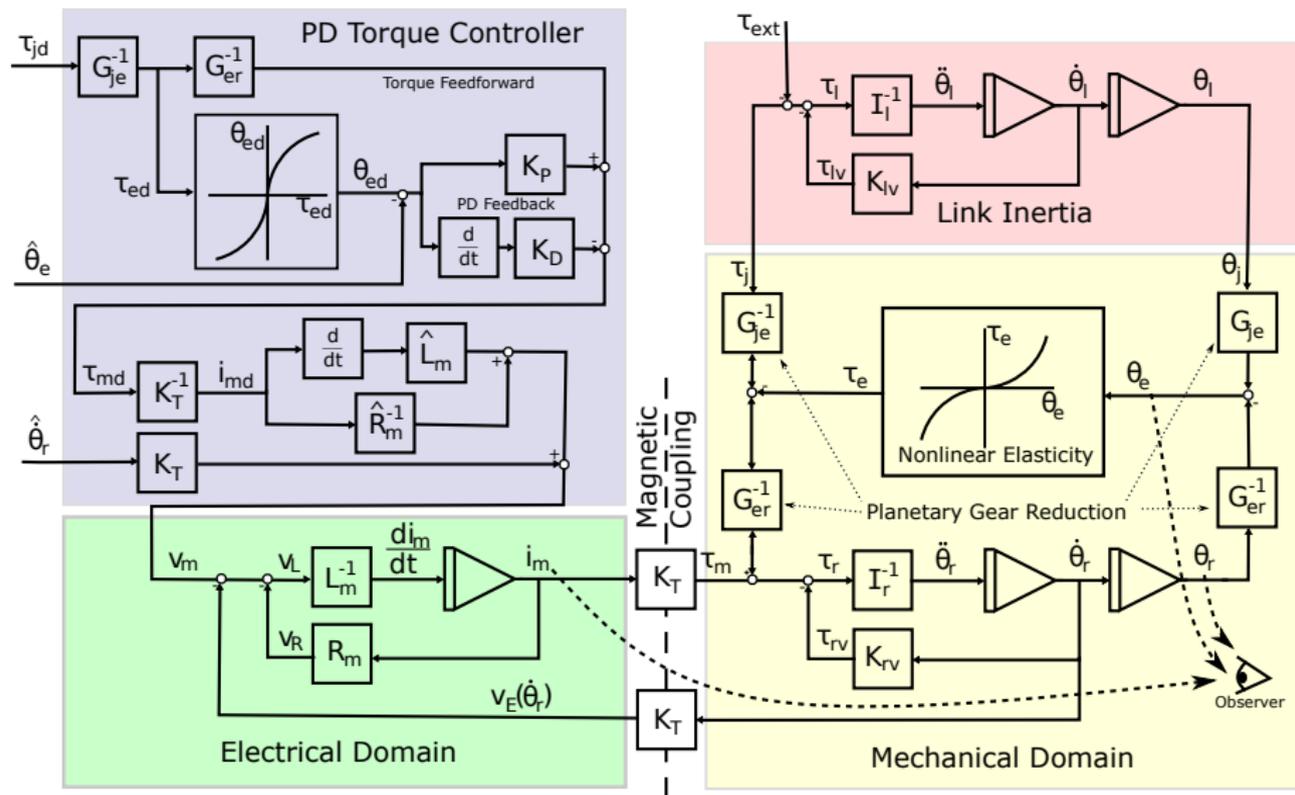
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HYPOSEA TORQUE CONTROLLER



SUMMARY OF ACTUATION

- ▶ Hypocycloid mechanism makes the best use of limited rotor torque by closely matching the expected joint torques of running.
- ▶ HypoSEA-v2 is light enough to use in a robot.
- ▶ Bigger motor drivers would improve peak torques.

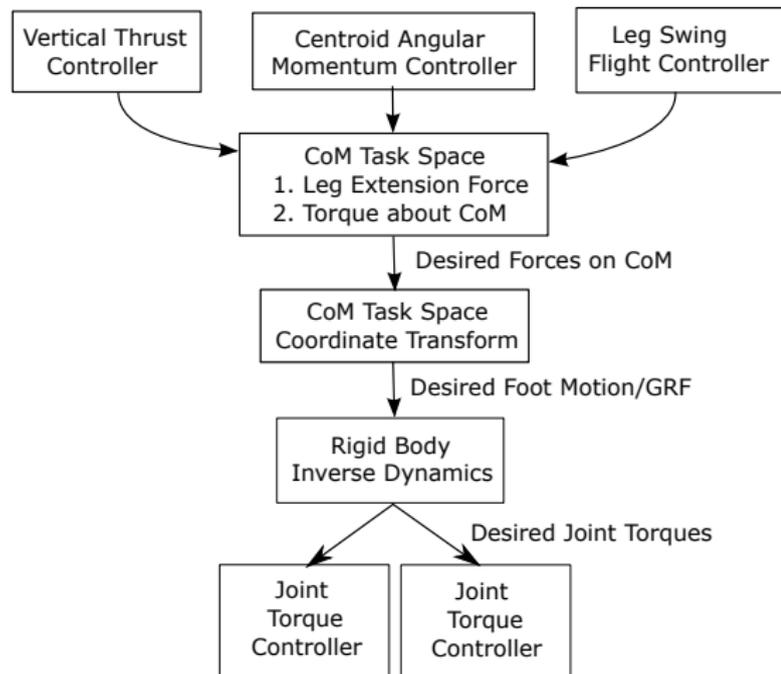
Let's now turn to JIMI's balancing controller, which sends signals to the joint torque controllers.

PART III: DYNAMIC BALANCING

Goal: To describe a centroidal task-space controller that creates a sinusoidal vertical GRF and stabilizes the centroidal angular momentum.

Overview:

1. Model of JIMI
2. Inverse Dynamics
3. Centroid Task Space
4. Dynamic Balance Controllers
5. Simulation Results



JIMI: A MONOPOD RUNNER

EQUATIONS OF MOTION

$$\mathbf{M}(\mathbf{q})\ddot{\mathbf{q}} + \mathbf{C}(\dot{\mathbf{q}}, \mathbf{q})\dot{\mathbf{q}} + \mathbf{g}(\mathbf{q}) = \mathbf{D}_j\tau_j + \mathbf{J}_f\lambda_f$$

DEFINITIONS

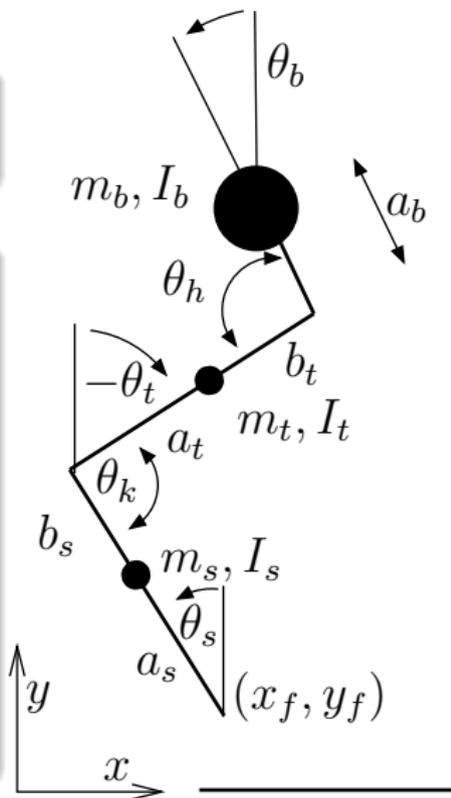
$$\mathbf{q} = [\theta_s \quad \theta_t \quad \theta_b \quad x_f \quad y_f]^T$$

$$\tau_j = [\tau_k \quad \tau_h]^T$$

$$\lambda_f = [F_{fx} \quad F_{fy}]^T$$

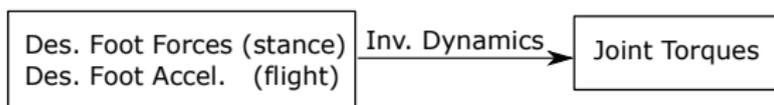
$$\mathbf{J}_f = \begin{bmatrix} 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}^T$$

$$\mathbf{D}_j = \begin{bmatrix} -1 & 1 & 0 & 0 & 0 \\ 0 & -1 & 1 & 0 & 0 \end{bmatrix}^T$$



INVERSE DYNAMICS GRF CONTROL

Goal: To solve for joint torques that give the desired GRF during stance, and the desired foot acceleration during flight.



STANCE INVERSE DYNAMICS (DES. FOOT GRFs: $\lambda_f = \lambda_{fd}$)

$$\begin{bmatrix} \mathbf{M} & \mathbf{J}_f^T & -\mathbf{D}_j^T \\ \mathbf{J}_f & \mathbf{0} & \mathbf{0} \\ 0 & \mathbf{I} & 0 \end{bmatrix} \begin{bmatrix} \ddot{\mathbf{q}} \\ -\lambda_f \\ \tau_{jd} \end{bmatrix} = \begin{bmatrix} \tau_v - \mathbf{C}\dot{\mathbf{q}} - \mathbf{g} \\ -\mathbf{J}_f\dot{\mathbf{q}} \\ -\lambda_{fd} \end{bmatrix}$$

FLIGHT INVERSE DYNAMICS (DES. FOOT MOTION: $\mathbf{J}_f\ddot{\mathbf{q}} = \ddot{\mathbf{q}}_{fd}$)

$$\begin{bmatrix} \mathbf{M} & -\mathbf{D}^T \\ \mathbf{J}_f & \mathbf{0} \end{bmatrix} \begin{bmatrix} \ddot{\mathbf{q}} \\ \tau_{jd} \end{bmatrix} = \begin{bmatrix} \tau_v - \mathbf{C}\dot{\mathbf{q}} - \mathbf{g} \\ \ddot{\mathbf{q}}_{fd} \end{bmatrix}$$

CENTROID TASK SPACE

Use horizontal GRF to control centroidal torque:

CENTROIDAL TORQUE TO HORIZ. GRF

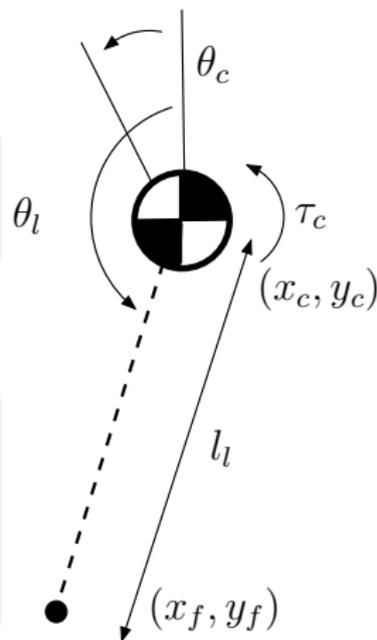
$$F_{fx}(F_{fy}, \tau_c) = \frac{(x_c - x_f)F_{fy} - \tau_c}{(y_c - y_f)}$$

Express controllers in CoM-Foot polar coords:

POLAR COORDINATES

$$\theta_l = \tan^{-1} \frac{x_c - x_f}{y_c - y_f}$$

$$l_l = \sqrt{(x_c - x_f)^2 + (y_c - y_f)^2}$$



3-PART DYNAMIC BALANCING CONTROLLER

SINUSOIDAL VERTICAL GRF

$$y_R(t) = \hat{y}_{cTD} + \frac{hRt}{T_S}$$

$$F_{fy}(t) = K_{cR}(y_R - \hat{y}_c)$$

CENTROIDAL ANGULAR MOMENTUM

$$\theta_c = K_{lb}\theta_b - \theta_l + \theta_{b0}$$

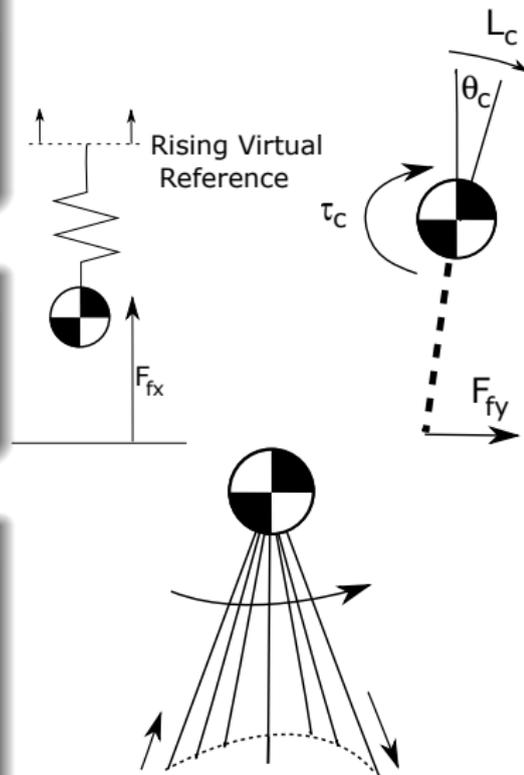
$$\tau_c = K_{cP}\theta_c + K_{cD}L_c$$

LEG SWING AND CoP CONTROL

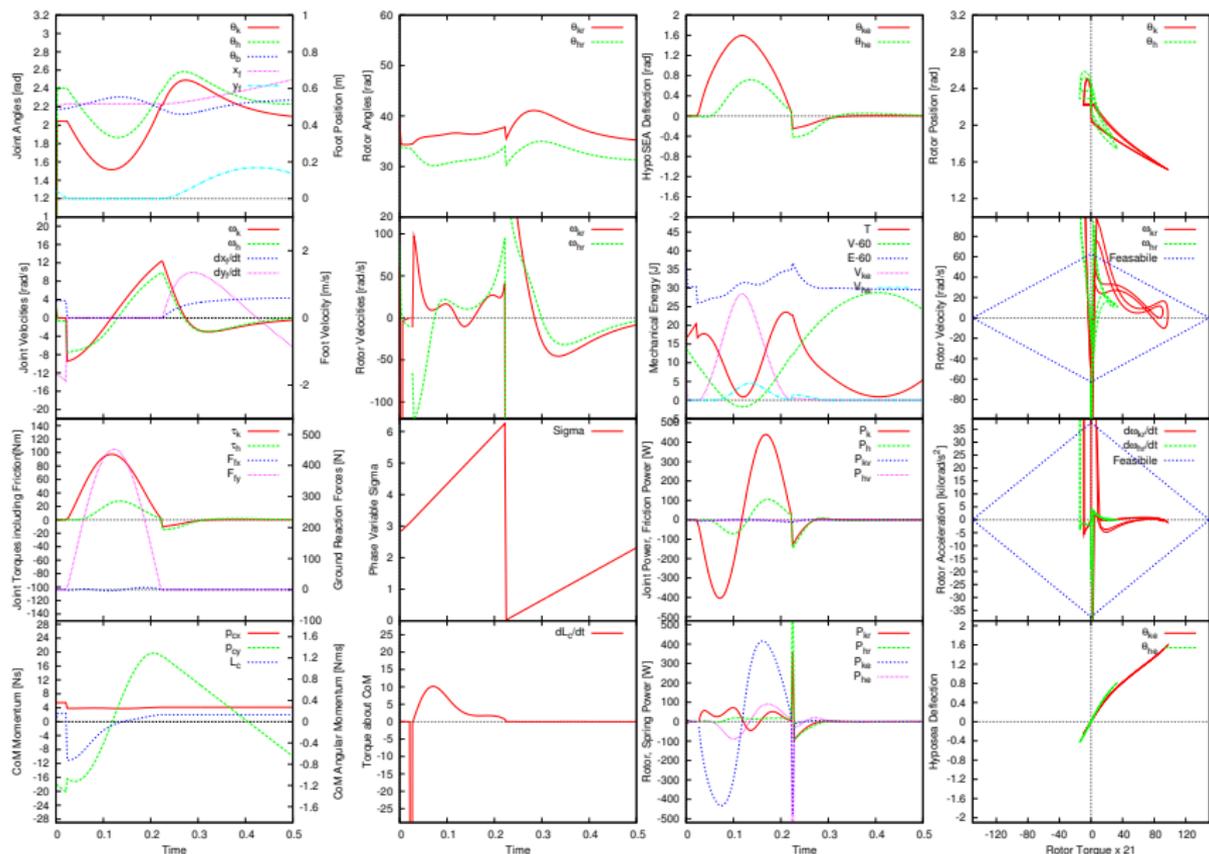
$$\sigma = \pi(t - t^{LO})/T^F + \frac{\pi}{2}$$

$$\theta_{ld}(\sigma) = K_1 \sin(\sigma + \frac{\pi}{2}) + K_2$$

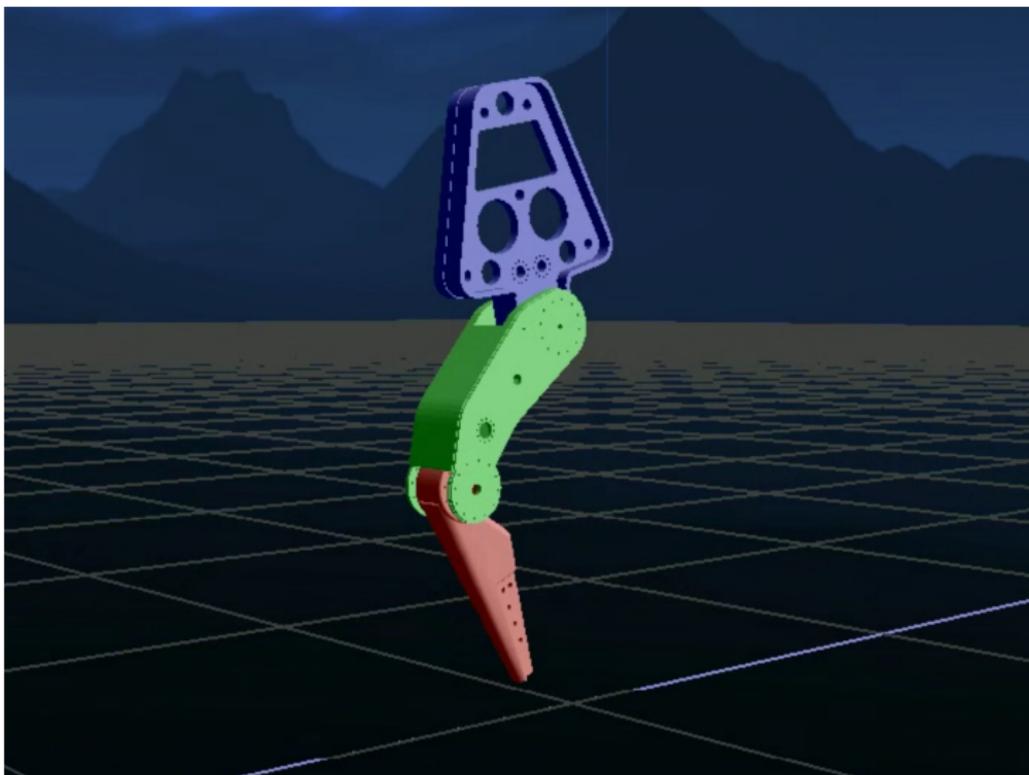
$$l_{ld}(\sigma) = K_3(\sin(\sigma) + \sin(2\sigma)) + K_4$$



SIMULATION RESULTS



OLD SIMULATION VIDEO



SUMMARY OF DYNAMIC BALANCING CONTROLLER

- ▶ JIMI, HypoSEA, and controller dynamics were studied in simulation *during the design process*.
- ▶ Three rules expressed in centroid task space stabilize the robot.
- ▶ Rotor work was minimized by matching passive mechanical dynamics and controller torques.

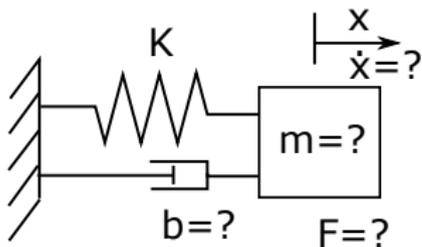
Next: How can we estimate state and model parameters for the above model-based control?

PART IV: STATE AND MODEL ESTIMATION

Goal: To describe how the state and model parameters of the JIMI were estimated using model-based least squares regression with power constraints.

1. Example: Numerical Differentiation
2. Model-based Estimation
3. HypoSEA State Observer
4. JIMI State Observer

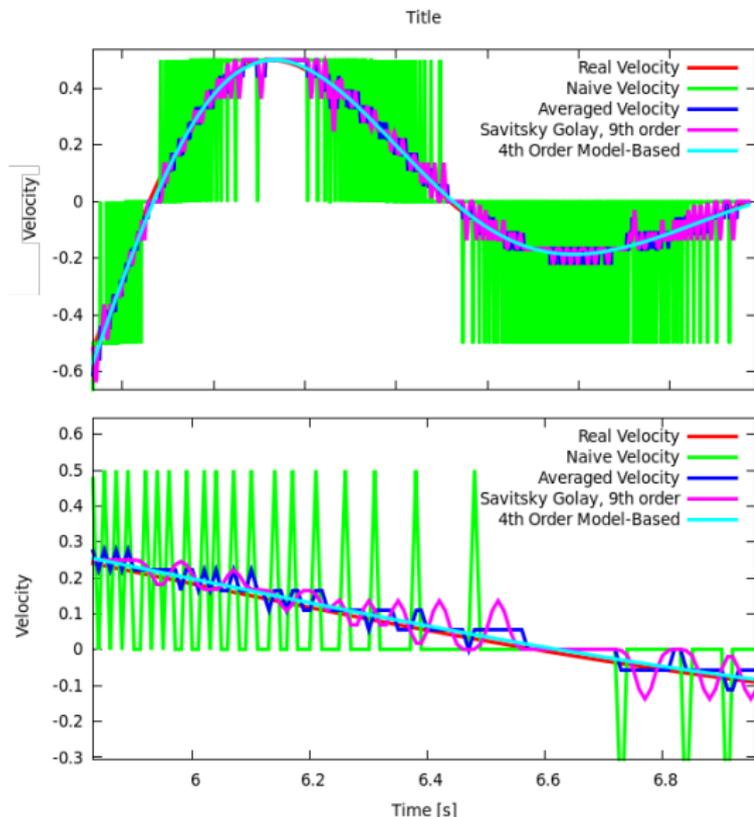
NUMERICAL DERIVATIVES OF NOISY DATA



Ways to differentiate:

- ▶ Real value
- ▶ Finite differences
- ▶ Averaging/LF pass
- ▶ Polynomial Regression
- ▶ Model-based

If models can improve *control*,
models can improve *estimation*!



MODEL-BASED ESTIMATION

LINEAR ODE MODEL

$$\dot{x} = Ax + Bu + \delta$$

$$y = Cx + \epsilon$$

States x , observations y ,
input u , noise δ and ϵ .

- ▶ For realtime control, estimators must be causal – Kalman Filter and its variants work great.
- ▶ But for smoothed past values, central differences better.
- ▶ JIMI uses model-based fourth-order central-difference weighted least squares.

KALMAN FILTER, UNROLLED, VARIANCE WEIGHTS HIDDEN

$$\begin{bmatrix} C & & & \\ -dt(I + A) & I & & \\ & C & & \\ & -dt(I + A) & I & \\ & & & C \end{bmatrix} \begin{bmatrix} x_0 \\ x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} y_0 \\ Bu_0 \\ y_1 \\ Bu_1 \\ y_2 \end{bmatrix}$$

KALMAN FILTERS WITH FATTER BANDS

KALMAN FILTER DIFFERENCES MATRIX

$$\begin{bmatrix} \dot{x}_0 \\ \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \\ \dot{x}_4 \\ \vdots \end{bmatrix} = \frac{1}{h} \begin{bmatrix} -1 & 1 & & & & \\ & -1 & 1 & & & \\ & & \ddots & \ddots & & \\ & & & -1 & 1 & \\ & & & & & \ddots \end{bmatrix} \begin{bmatrix} x_0 \\ x_1 \\ x_2 \\ x_3 \\ x_4 \\ \vdots \end{bmatrix}$$

4TH ORDER DISCRETE DIFFERENCES MATRIX

$$\begin{bmatrix} \dot{x}_0 \\ \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \\ \dot{x}_4 \\ \vdots \end{bmatrix} = \frac{1}{12h} \begin{bmatrix} 0 & 8 & -1 & & & \\ -8 & 0 & 8 & \ddots & & \\ 1 & -8 & \ddots & 8 & -1 & \\ & \ddots & -8 & 0 & 8 & \\ & & 1 & -8 & 0 & \end{bmatrix} \begin{bmatrix} x_0 \\ x_1 \\ x_2 \\ x_3 \\ x_4 \\ \vdots \end{bmatrix}$$

JIMI'S MODEL-BASED FIXED-LAG SMOOTHING

4TH ORDER DISCRETE DIFFERENCES MATRIX

$$\begin{bmatrix} \text{diag}(C, C, \dots) \\ \text{diag} \left[-\frac{1}{12}I \quad \frac{2}{3}I \quad -dtA \quad -\frac{2}{3}I \quad \frac{1}{12}I \right] \end{bmatrix} \begin{bmatrix} x_0 \\ x_1 \\ x_2 \\ x_3 \\ x_4 \\ \vdots \end{bmatrix} = \begin{bmatrix} y_0 \\ y_1 \\ y_2 \\ y_3 \\ y_4 \\ \vdots \\ Bu \end{bmatrix}$$

MODEL PARAMETER ESTIMATION

Problem: How can we estimate model parameters $\dot{x} = Ax + Bu$?

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Observation: If your model is good, excluding external disturbances, the power in and out of the system will be zero from state to state.

MODEL PARAMETER ESTIMATION

Problem: How can we estimate model parameters $\dot{x} = Ax + Bu$?

Observation: If your model is good, excluding external disturbances, the power in and out of the system will be zero from state to state.

Solution: Least squares parameter estimation minimizing power error.

- ▶ Uses energy as a lingua franca between different physical parameters.
- ▶ Expand terms of A, B matrices; use to write power balance equation.

$$\begin{bmatrix} \dot{x}_0 \\ \dot{x}_1 \\ \vdots \\ \dot{x}_n \end{bmatrix} = \begin{bmatrix} \phi_{11} & \phi_{12} & \cdots & \phi_{1n} \\ \phi_{21} & \phi_{22} & & \\ \vdots & & \ddots & \\ \phi_{n1} & & & \phi_{nn} \end{bmatrix} \begin{bmatrix} x_0 \\ x_1 \\ \vdots \\ x_n \end{bmatrix} + \begin{bmatrix} \gamma_{11} & \gamma_{12} & \cdots & \gamma_{1n} \\ \gamma_{21} & \gamma_{22} & & \\ \vdots & & \ddots & \\ \gamma_{n1} & & & \gamma_{nn} \end{bmatrix} \begin{bmatrix} u_0 \\ u_1 \\ \vdots \\ u_n \end{bmatrix}$$

Let $\phi = [\phi_1 \quad \phi_2 \quad \cdots \quad \gamma_1 \quad \gamma_2 \quad \cdots]^T$ and $P_{err}(x, \dot{x}, u) = U\phi$, and Q be weights.

$$\hat{\phi} = (U^T Q U)^{-1} U^T Q P_{err}$$

SUMMARY OF STATE ESTIMATION

- ▶ HypoSEA real time control uses a Kalman Filter.
- ▶ Smoothing is done with a higher order model-based filter.
- ▶ From smoothed data, we can iteratively improve $\hat{\phi}$ such that power is conserved.
- ▶ JIMI's inertial parameters not yet estimated.

Next: In what manner was this software written?

PART V: ASYNCHRONOUS, DATAFLOW PROGRAMMING

Goal: To present the programming style used to write the control software for JIMI, in the Clojure Language invented by Rich Hickey.

1. Why Another Robotics Software System?
2. Immutable Data and Pure Functions
3. Basics of Dataflow Programming
4. Advantages of Dataflow Programming
5. Screenshots of Developed Software
6. A Short Video

MOTIVATION: TO BE LESS IRRITATED

Irritation

Solution

Software licenses

Liberty-based software only

Xenomai + RoboLLI crashing my PC

Ordinary Linux Kernel + JVM

Recompiling on every code change

Dynamic language, JIT compilation

Not using all my CPU cores

Concurrent dataflow model

Inter-process communication barriers

Use many threads in one process

Bugs in one thread stopping others

Contain exceptions to each dataflow

Lack of real-time visualization

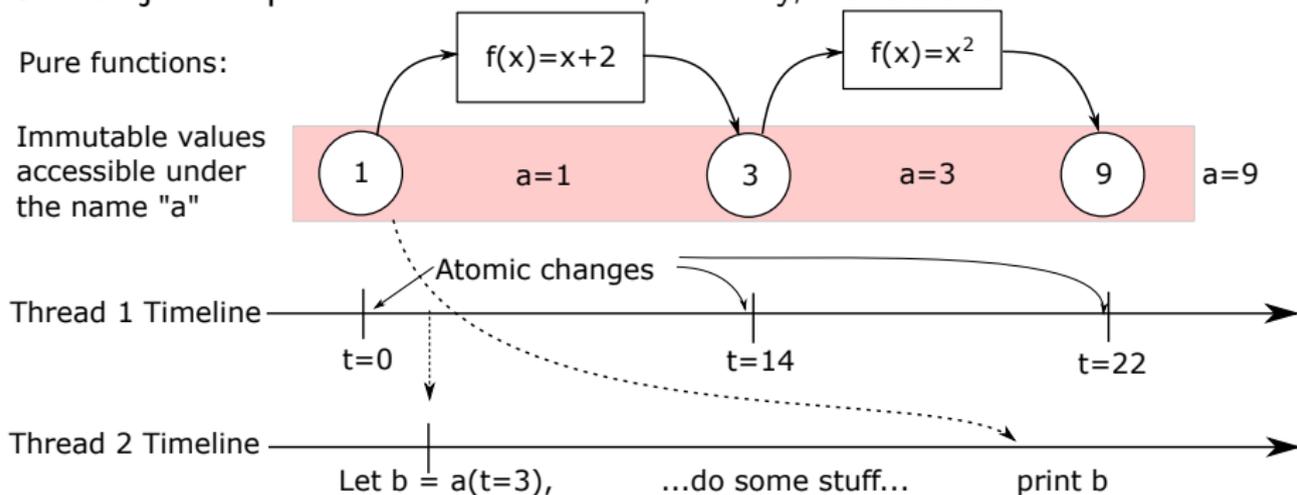
DIY oscilloscope, OpenGL viewer

Integrating non-synchronous data streams

Asynchronous, event-based code

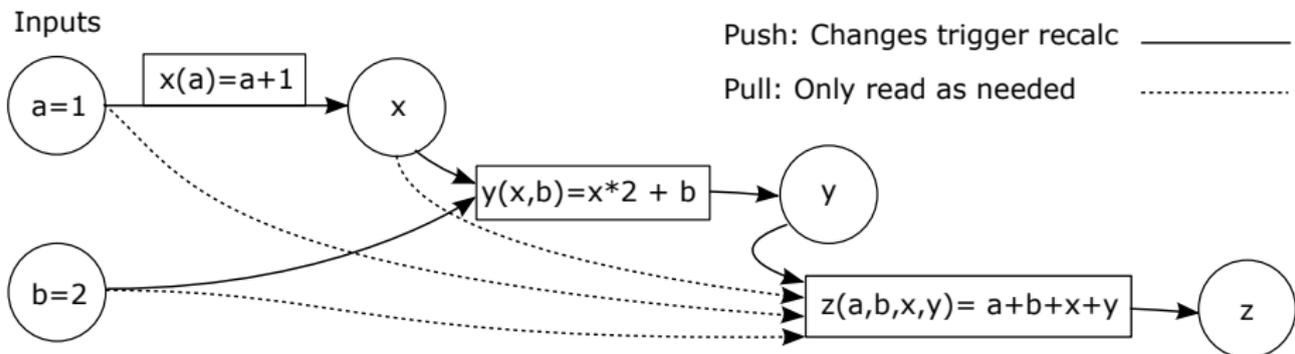
IMMUTABLE DATA & PURE FUNCTIONS (*Hickey*)

Use Clojure's epochal model of state, identity, transitions:



- ▶ Values are only birthed and GC'd – never modified.
- ▶ Names only point to one value at a time.
- ▶ Multiple threads can share same data.
- ▶ Tree structures can safely reuse old data to reduce copying.

DATAFLOW PROGRAMMING



- ▶ Data keeps itself updated!
- ▶ Always safe to read!
- ▶ Bugs isolated to each flow!
- ▶ Add new flows anytime!

DATAFLOW PROGRAMMING

Real applications need a few more details:

TRIGGERING If events occur faster than they can be processed, you can allow skipping of intermediate values.

PERIODICITY Achieved with scheduler that triggers functions.

COORDINATION Coordinating several references possible with software transactional memory (but I discourage it).

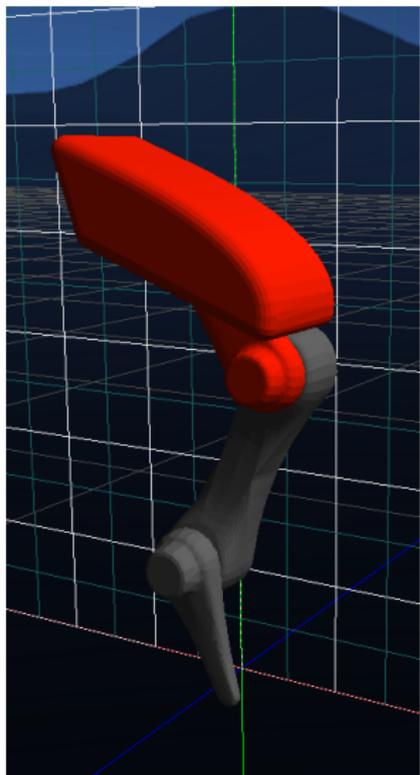
LATENCY Long chains of light computations can be forced to use same thread.

NEED-BASED Really expensive computations can be evaluated lazily, only as needed, and with most recent values.

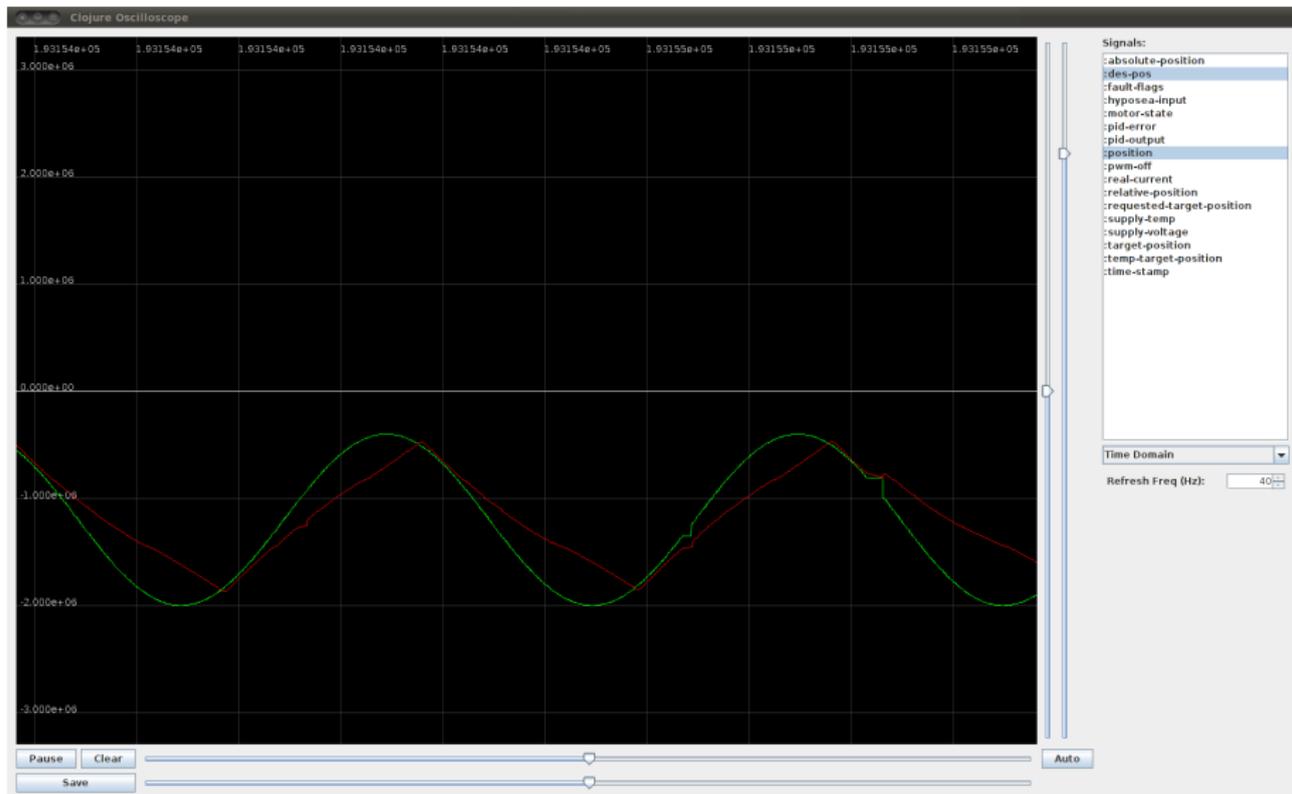
THREADING Queue arguments, execute function in a thread pool.

GENERALITY Useful to separate dependencies and recalculation trigger condition with another function.

SCREENSHOTS: OpenGL VIEWPORT



SCREENSHOTS: OSCILLOSCOPE



SCREENSHOTS: MOTOR CONTROLLER GUI

Motor Board Viewer:Hip

MOVE
STOP

IP address: 169.254.89.72
Board name: Hip

Input: Sine Bounce

Desired Pos. -1856338
PWM Offset 0
HypoSEA Pos. -648719

Configuration: Enable Bcast

Load Config
Save Config

Send Config
Request Cfg

Display Config

BCast Per [half-ms] 2
Current Limit [mA] 12,000
Absolute Zero 0
Min Position -3,000,000
Max Position 3,000,000
Pos P Gain 100,000
Pos I Gain 0
Pos D Gain 0

HypoSEA Observer

Mode: joystick 1

Desired q_e 0.00000
Desired Torque 0
Output Des-pos -859642

Load Cfg
Save Cfg

Deflection Offset -23
Position Offset 0
G1 Reduction 17
G2 Reduction -1
K_T Torque 0.3
L_m Inductance 0.003
R_m Resistance 2.64
J_r Inertia 0
J_l Inertia 0.001
b_r Visc. Fric. 0.01
b_l Visc. Fric. 0.01
l_l CoM Length 0.012
m_l Mass 5.3
K_e Spring 10,000
r Radius 0.025
p Pretension 0.01
K_stp Coeff. 0.5
q_lmax Limit 0.1
q_lmin Limit -1.8

ESTIMATED VALUES:

q_r	-8.59642
dq_r	0.00000
ddq_r	0.00000
q_l	-0.50567
dq_l	0.00000
ddq_l	0.00000
q_e	0.00000
dq_e	0.00000
t_e	0.00000
t_g	0.28963
t_ext	0.00000
v_s	25.63200
v_a	0.00000
i_m	0.26400
di_m	2.00000

P_s Supply Work	0.00000
P_R Resistance	0.20110
P_L Inductance	-0.00305
P_m EMF Work	0.00000
P_r Rotor Inertia	-0.00000
P_fr Rotor Fric.	-0.00000
P_er Rotor Elast.	-0.00000
P_el Link Elast	0.00000
P_fl Link Fric.	0.00000
P_g Gravity	0.00000
P_l Link inertia	0.00000
P_e Elastic	0.00000
P_ext external	0.00000

Total Error	0.18254
Electrical	-0.18254
Rotor	-0.00000
Link	0.00000
Spring	0.00000

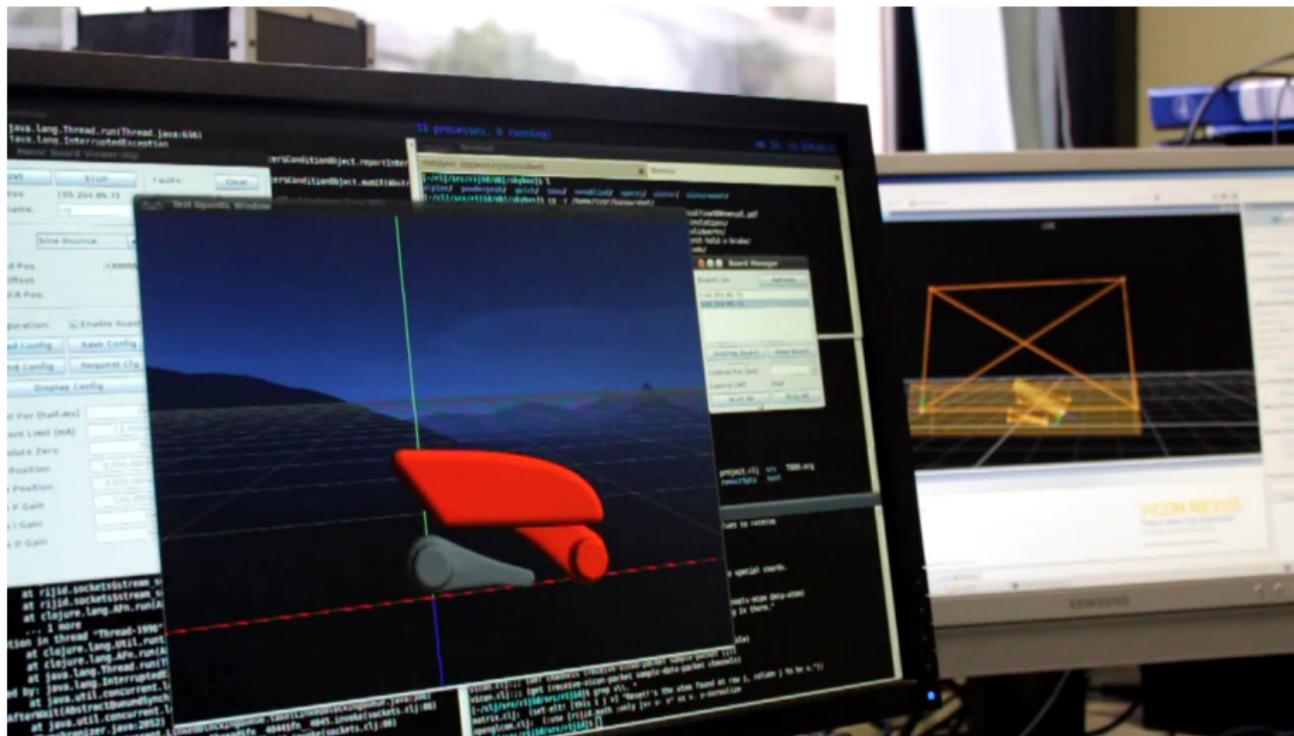
Faults: Clear

Overcurrent? 0
Overtemp? 0
Overvoltage? 0
Motor Stall? 0
Emerg. Stop? 0

Position 519865
Velocity
Torque
PID Output 0
PID Error 0
Current
Temp in C 66
V_Supply 25566
Time stamp 134321
Faults 0

Analog A
Analog B
Deflection -199
Quick Speed
Motor State 512
Real Current 0
Relative Pos 0
Target Pos -1669457
Temp Targ Pos -687859
Req Targ Pos -1669457
Twin Pos

20 SECONDS OF VIDEO



SUMMARY OF SOFTWARE ARCHITECTURE

- ▶ Clojure is beautiful, lisp-y, functional, and uniquely immutable.
- ▶ Dataflow allows great concurrency and is very simple.
- ▶ Latency is pretty good (100uS), would improve if optimized.
- ▶ Incremental, realtime GC badly needed to stop erratic 5ms pauses.
- ▶ Prioritization didn't work well (JVM thread priorities broken).

The latter two problems would probably be solved by a realtime JVM.

PART VI: ADVANCED COMPOSITE MATERIALS

Goal: To present the monocoque Carbon Fiber Reinforced Polymer (CFRP) construction techniques used to make JIMI, and show they are accessible to researchers at IIT.

Overview:

1. Monocoque structures
2. Composite Sandwich Structures
3. Composite Layup Techniques
4. Construction Photos



MONOCOQUE (“SINGLE SHELL”) STRUCTURES

A very lightweight way to create stiff, load-carrying skins with complex shapes.

Benefits:

- ▶ Extremely light, strong, and stiff
- ▶ One molded part can replace several interconnected parts

Disadvantages:

- ▶ Generally not machinable, threadable without metal embedments
- ▶ Requires time-consuming mold-making
- ▶ Very anisotropic strength properties
- ▶ Hard to mass-produce

Internal truss structure:

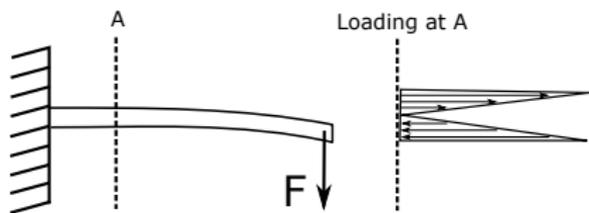


Monocoque CFRP structure:



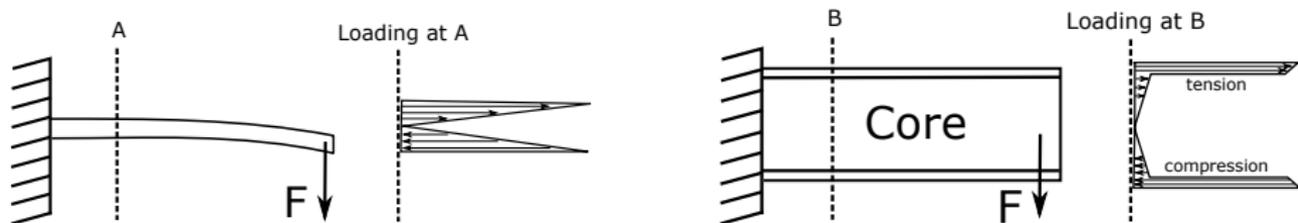
COMPOSITE SANDWICH STRUCTURES

Problem: How can a thin skin carry a load without being too flexible?



COMPOSITE SANDWICH STRUCTURES

Problem: How can a thin skin carry a load without being too flexible?



Solution: Make a sandwich structure.

- ▶ Core materials have only low shear load
- ▶ Low density cores add almost no weight
- ▶ Effective stiffness, strength increased
- ▶ Balsa wood, plastic foams, aramid or metal honeycombs common in aircraft



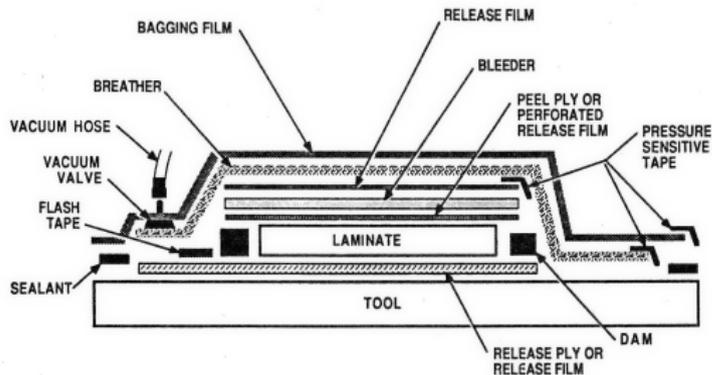
BASIC WET LAYUP

- ▶ Essentially just “painting strong fibers with plastic glue”.
- ▶ Simple, requires few tools, but makes heavier parts with bad finishes

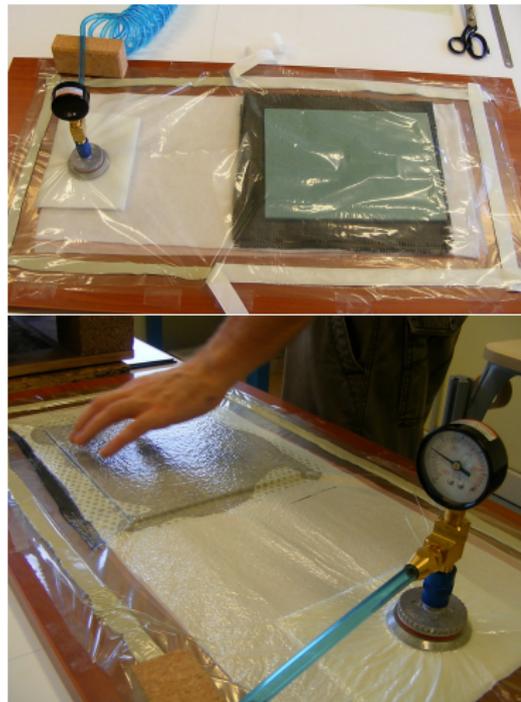


VACUUM BAG LAYUP

- ▶ Use atmospheric pressure to squeeze out unneeded resin, compress fibers
- ▶ Accessible technique for amateurs



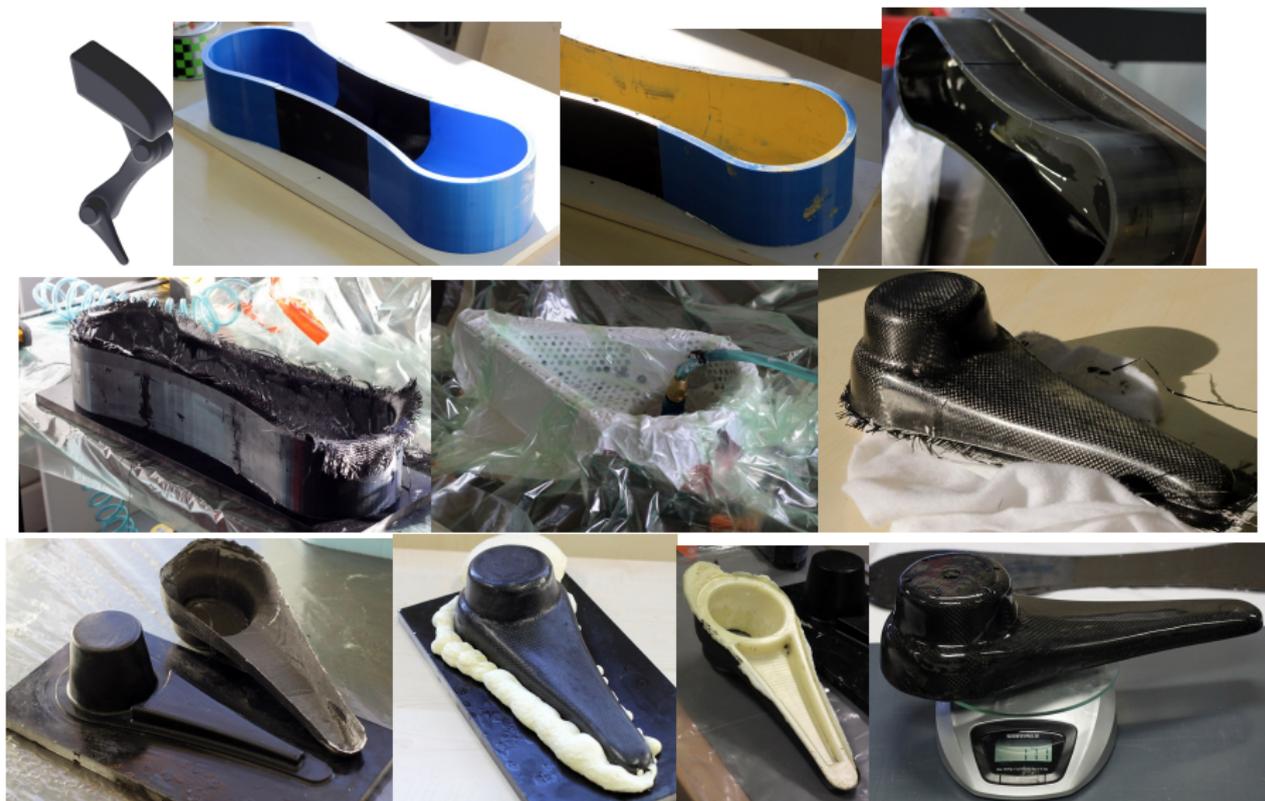
LAYUP SEQUENCE FOR BAGGING OPERATION



MOLDLESS COMPOSITE PARTS



DOUBLY-MOLDED COMPOSITE SANDWICH PARTS



SUMMARY

- ▶ Carbon fiber sandwich structures are uniquely lightweight and stiff.
- ▶ JIMI's CFRP structure was constructed entirely at IIT.
- ▶ JIMI's three parts took ~160-200 hours of work.
- ▶ Shank mass: 171g
- ▶ Thigh mass: 518g
- ▶ Body mass: 976g (Moldless construction)

Caution: Please learn safe handling procedures before trying it yourself!

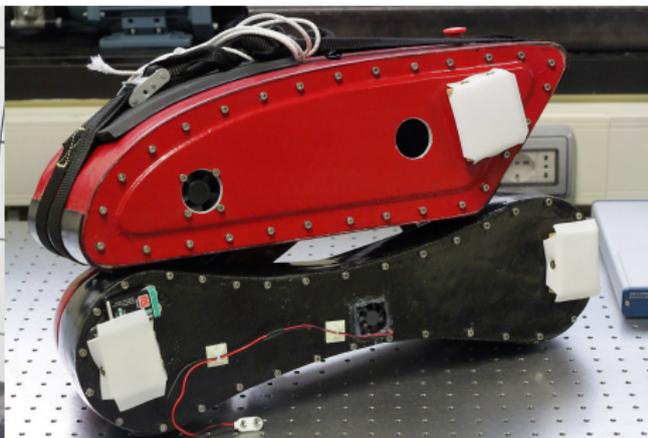
PROJECT CONCLUSIONS

Goal: To show photos and summarize the results in 90 seconds.

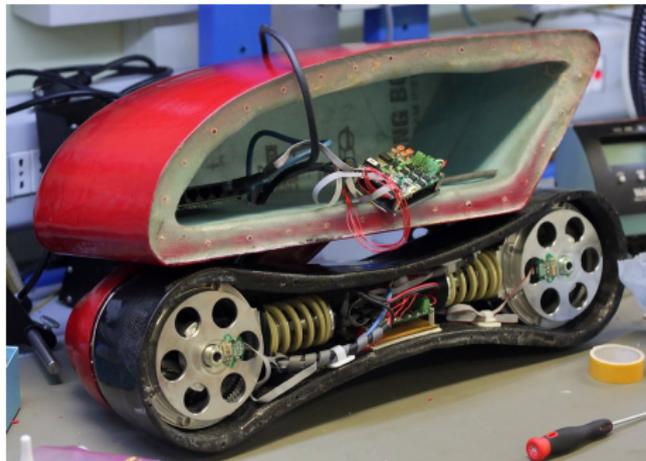
1. JIMI Photo Summary
2. Successes and Failures
3. Future Work



JIMI PHOTO SUMMARY 1



JIMI PHOTO SUMMARY 2



SUCCESSSES AND FAILURES

Successes:

- ▶ Basic concept works: match actuation, control to dynamics

Failures:

- ▶ Irregular vicon latency (TCP) a problem at present
- ▶ Joint torques not yet optimal as in simulation

SUCCESSSES AND FAILURES

Successes:

- ▶ Basic concept works: match actuation, control to dynamics
- ▶ Asynchronous dataflow control is robust, easy to debug

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SUCCESSSES AND FAILURES

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- ▶ Asynchronous dataflow control is robust, easy to debug
- ▶ CFRP pieces are lightweight

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- ▶ Hard to disassemble JIMI

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- ▶ Asynchronous dataflow control is robust, easy to debug
- ▶ CFRP pieces are lightweight
- ▶ HypoSEA-v2 controls force well

Failures:

- ▶ Irregular vicon latency (TCP) a problem at present
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- ▶ GRF controller has a singularity
- ▶ Hard to disassemble JIMI
- ▶ Need more powerful motor drivers badly

SUCCESSSES AND FAILURES

Successes:

- ▶ Basic concept works: match actuation, control to dynamics
- ▶ Asynchronous dataflow control is robust, easy to debug
- ▶ CFRP pieces are lightweight
- ▶ HypoSEA-v2 controls force well
- ▶ Energy regeneration a bonus

Failures:

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- ▶ GRF controller has a singularity
- ▶ Hard to disassemble JIMI
- ▶ Need more powerful motor drivers badly

FUTURE WORK

There are several research directions that could be pursued from here:

PERFORMANCE: How fast/high can JIMI be made to run/jump?

SOFTWARE: Clean up, document, and release the dataflow software.

MECHANICAL: Can the torso be rebuilt lighter?

ACTUATION: Can bigger motor drivers improve HypoSEA performance?

ENERGETIC: What trajectories maximize energy recovery?

COMMERCIAL: Does the HypoSEA have any economic value?

From now until August, there is only time for me to pursue the first.

Is anybody interested in using JIMI or the HypoSEA-v1 in the future?

Special thanks to

Gianluca Pane

Phil Hudson

Dr. Nikos Tsagarakis

Dr. Darwin Caldwell
and the HyQ Group

Thank you all for your attention.

Questions welcome!

